

Diodes

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I. WHY

Diodes are a magical ¹ semiconductor device that conduct current in one direction. It's one of the fundamental electronics components, and it's a good idea to understand how they work.

If you don't understand diodes, then you won't understand transistors, neither bipolar, or field effect transistors.

A useful feature of the diode is the exponential relationship between the forward current, and the voltage across the device.

To understand why a diode works it's necessary to understand the physics behind semiconductors.

This paper attempts to explain in the simplest possible terms how a diode works ²

II. SILICON

Integrated circuits use single crystalline silicon. The silicon crystal is grown with the [Czochralski method](#) which forms a ingot that is cut into wafers. The wafer is a regular silicon crystal, although, it is not perfect.

A silicon crystal unit cell, as seen in Figure 1 is a diamond faced cubic with 8 atoms in the corners spaced at 0.543 nm, 6 at the center of the faces, and 4 atoms inside the unit cell at a nearest neighbor distance of 0.235 nm.

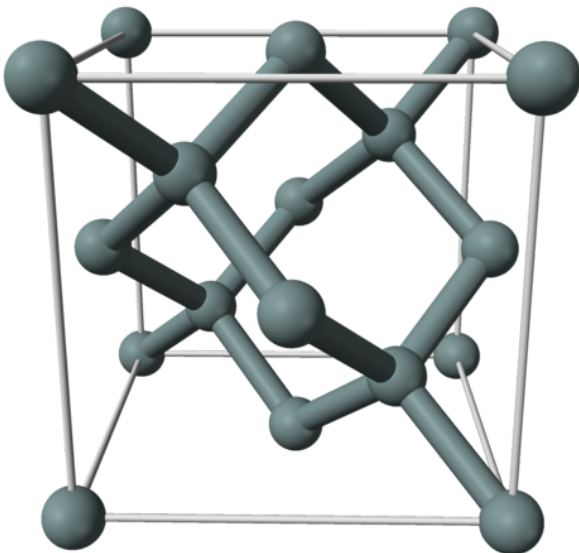


Figure 1: Silicon crystal unit cell

As you hopefully know, the energy levels of an electron around a positive nucleus are quantized, and we call them orbitals (or shells). For an atom far away from any others, these orbitals, and energy levels are distinct. As we bring atoms closer together, the orbitals start to interact, and in a crystal, the distinct orbital energies split into bands of allowed energy states. No two electrons, or any Fermion (spin of 1/2), can occupy the same quantum state. We call the outermost "shared" orbital, or band, in a crystal the valence band. Hence covalent bonds.

If we assume the crystal is perfect, then at 0 Kelvin all electrons will be part of covalent bonds. Each silicon atom share 4 electrons with its neighbors. What we really mean when we say "share 4 electrons" is that the wave-functions of the outer orbitals interact, and we can no longer think of the orbitals as belonging to either of the silicon nuclei. All the neighbors atoms "share" electrons, and nowhere is there an vacant state, or a hole, in the valence band.

If such a crystal were to exist, where there were no holes in the valence band, and a net neutral charge, the crystal could not conduct any drift current. Electrons would move around continuously, swapping states, but there could be no net drift of charge carriers.

In an atom, or a crystal, there are also higher energy states where the carriers are "free" to move. We call these energy levels, or bands of energy levels, conduction bands. In singular form "conduction band", refers to the lowest available energy level where the electrons are free to move.

Due to imperfectness of the silicon crystal, and non-zero temperature, there will be some electrons that achieve sufficient energy to jump to the conduction band. The electrons in the conduction band leave vacant states, or holes, in the valence band.

Electrons can move both in the conduction band, as free electrons, and in the valence band, as a positive particle, or hole. Both bands can support drift and diffusion currents.

III. INTRINSIC CARRIER CONCENTRATION

The intrinsic carrier concentration of silicon, or the density of free electrons and holes at a given temperature, is given by

$$n_i = \sqrt{N_c N_v} e^{-E_g/(2kT)} \quad (1)$$

where E_g is the bandgap energy of silicon (approx 1.12 eV), k is Boltzmann's constant, T is the temperature in Kelvin, N_c is

¹It doesn't stop being magic just because you know how it works. Terry Pratchett, The Wee Free Men

²Simplify as much as possible, but no more. Einstein

the density of states in conduction band, and N_v is the density of states in the valence band.

The density of states are

$$N_c = 2 \left[\frac{2\pi kT m_n^*}{h^2} \right]^{3/2} \quad N_v = 2 \left[\frac{2\pi kT m_p^*}{h^2} \right]^{3/2}$$

where h is Planck's constant, m_n^* is the effective mass of electrons, and m_p^* is the effective mass of holes.

Leave it to engineers to simplify equations beyond understanding. Equation (1) is complicated, and the density of states includes the effective mass of electrons and holes, which is a parameter that depends on the curvature of the band structure. To engineers, this is too complicated, and n_i has been simplified so it “works” in daily calculation.

Through engineering simplification, however, physics understanding is lost.

In [1] they claim the intrinsic carrier concentration is a constant, although they do mention n_i doubles every 11 degrees Kelvin.

In BSIM 4.8 [2] the intrinsic carrier concentration is

$$n_i = 1.45e10 \frac{TNOM}{300.15} \sqrt{\frac{T}{300.15}} \exp^{21.5565981 - \frac{E_g}{2kT}}$$

Comparing the three models in Figure 2, we see the shape of BSIM and the full equation is almost the same, while the “doubling every 11 degrees” is just wrong.

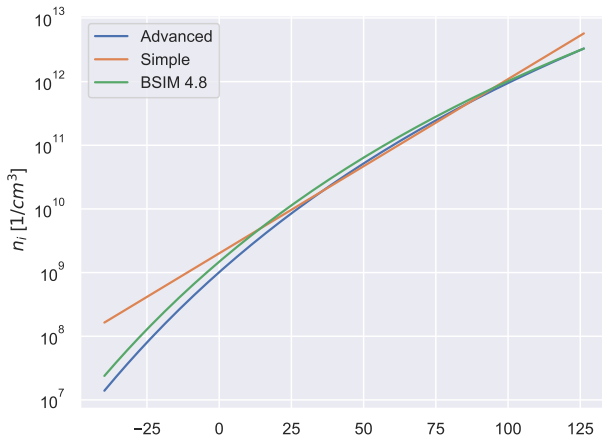


Figure 2: Intrinsic carrier concentration versus temperature

At room temperature the intrinsic carrier concentration is approximately $n_i = 1 \times 10^{16}$ carriers/m³.

That may sound like a big number, however, if we calculate the electrons per μm^3 it's $n_i = \frac{1 \times 10^{16}}{(1 \times 10^6)^3}$ carriers/ $\mu\text{m}^3 < 1$, so there are really not that many free carriers in intrinsic silicon.

From Figure 2 we can see that n_i changes greatly as a function of temperature, but the understanding “why” is not easy to

get from “doubling every 11 degrees”. To understand the temperature behavior of diodes, we must understand Eq (1).

So where does Eq (1) come from? I find it unsatisfying if I don't understand where things come from. I like to understand why there is an exponential, or effective mass, or Planck's constant. If you're like me, then read the next section. If you don't care, and just want to memorize the equations, or indeed the number of intrinsic carrier concentration number at room temperature, then skip the next section.

IV. IT'S ALL QUANTUM

There are two components needed to determine how many electrons are in the conduction band. The density of available states, and the probability of an electron to be in that quantum state.

For the density of states we must turn to quantum mechanics. The probability amplitude of a particle can be described as

$$\psi = Ae^{i(kr - \omega t)}$$

where k is the wave number, and ω is the angular frequency, and \mathbf{r} is a spatial vector.

In one dimension we could write $\psi(x, t) = Ae^{i(kx - \omega t)}$

In classical physics we described the Energy of the system as

$$\frac{1}{2m}p^2 + V = E$$

where $p = mv$, m is the mass, v is the velocity and V is the potential.

In the quantum realm we must use the Schrodinger equation to compute the time evolution of the Energy, in one space dimension

$$-\frac{\hbar^2}{2m} \frac{\partial^2}{\partial x^2} \psi(x, t) + V(x) \psi(x, t) = i\hbar \frac{\partial}{\partial t} \psi(x, t)$$

where m is the mass, V is the potential, $\hbar = h/2\pi$.

We could rewrite the equation above as

$$\hat{H}\psi(x, t) = i\hbar \frac{\partial}{\partial t} \psi(x, t) = \hat{E}\psi(x, t)$$

where \hat{H} is sometimes called the *Hamiltonian* and is an operator, or something that act on the wave-function. In [Feynman's Lectures on Physics](#) Feynman called the Hamiltonian the *Energy Matrix* of a system. I like that better. The \hat{E} is the energy operator, something that operates on the wave-function to give the Energy.

We could re-arrange

$$[\hat{H} - \hat{E}]\psi(r, t) = 0$$

This is an equation with at least 5 unknowns, the space vector in three dimensions, time, and the energy matrix \hat{H} .

The dimensions of the energy matrix depends on the system. The energy matrix further up is for one free electron. For an atom, the energy matrix will have more dimensions to describe the possible quantum states.

I consider all energy matrices as infinite dimensions, but most state transitions are so unlikely that they can be safely ignored.

I was watching [Quantum computing in the 21st Century](#) and David Jamison mentioned that the largest system we could today compute would be a system with about 30 electrons.

We know exactly how the equations of quantum mechanics appear to be, and they've proven extremely successful, we must make simplifications before we can predict how electrons behave in complicated systems like the silicon lattice with approximately 0.7 trillion electrons per cube micro meter. You can check the calculation

$$\left[\frac{1 \mu\text{m}}{0.543 \text{ nm}} \right]^3 \times 8 \text{ atoms per unit cell} \times 14 \text{ electrons per atom}$$

A. Density of states

To compute “how many Energy states are there per unit volume in the conduction band”, or the “density of states”, we start with the three dimensional Schrodinger equation for a free electron

$$-\frac{\hbar^2}{2m} \nabla^2 \psi = E \psi$$

I'm not going to repeat the computation here, but rather paraphrase the steps. You can find the full derivation in [Solid State Electronic Devices](#).

The derivation starts by computing the density of states in the k-space, or momentum space,

$$N(dk) = \frac{2}{(2\pi)^p} dk$$

Where p is the number of dimensions (in our case 3).

The band structure $E(k)$ is used to convert to the density of states to a function of energy $N(E)$. The simplest band structure, and an approximation of the lowest conduction band is

$$E(k) = \frac{\hbar^2 k^2}{2m^*}$$

where m^* is the effective mass of the particle. It is within this effective mass that we “hide” the complexity of the actual three-dimensional crystal structure of silicon.

The effective mass when we compute the density of states is

$$m^* = \frac{\hbar^2}{\frac{d^2 E}{dk^2}}$$

as such, the effective mass depends on the localized band structure of the silicon unit cell, and depends on direction of movement, strain of the silicon lattice, and probably other things.

In 3D, once we use the above equations, one can compute that the density of states per unit energy is

$$N(E)dE = \frac{2}{\pi^2} \frac{m^{*3/2}}{\hbar^2} E^{1/2} dE$$

In order to find the number of electrons, we need the probability of an electron being in a quantum state, which is given by the [Fermi-Dirac distribution](#)

$$f(E) = \frac{1}{e^{(E-E_F)/kT} + 1} \quad (2)$$

where E is the energy of the electron, E_F is the [Fermi level](#) or checmical potential, k is Boltzmann's constant, and T is the temperature in Kelvin.

Fun fact, the Fermi level difference between two points is what you measure with a voltmeter.

If the $E - E_F > kT$, then we can start to ignore the +1 and the probability reduces to

$$f(E) = \frac{1}{e^{(E-E_F)/kT}} = e^{(E_F-E)/kT}$$

A few observation on the Fermi-Dirac distribution. If the Energy of a state is at the Fermi level, then $f(E) = \frac{1}{2}$, or a 50 % probability of being occupied.

In a metal, the Fermi level lies within a band, as the conduction band and valence band overlap. As a result, there are a bunch of free electrons that can move around. Metal does not have the same type of covalent bonds as silicon, but electrons are shared between a large part of the metal structure. I would also assume that the location of the Fermi level within the band structure explains the difference in conductivity of metals, as it would determined how many electrons are free to move.

In an insulator, the Fermi level lies in the bandgap between valence band and conduction band, and usually, the bandgap is large, so there is a low probability of finding electrons in the conduction band.

In a semiconductor we also have a bandgap, but much lower energy than an insulator. If we have thermal equilibrium, no external forces, and we have an un-doped (intrinsic) silicon semiconductor, then the fermi level E_F lies half way between the conduction band edge E_C and the valence band edge E_V .

The bandgap is defined as the $E_C - E_V = E_g$, and we can use that to get $E_F - E_C = E_C - E_g/2 - E_C = -E_g/2$. This

is why the bandgap of silicon keeps showing up in our diode equations.

The number of electrons per delta energy will then be given by

$$N_e dE = N(E) f(E) dE$$

, which can be integrated to get

$$n_e = 2 \left(\frac{2\pi m^* kT}{h^2} \right)^{3/2} e^{(E_F - E_C)/kT}$$

For intrinsic silicon at thermal equilibrium, we could write

$$n_0 = 2 \left(\frac{2\pi m^* kT}{h^2} \right)^{3/2} e^{-E_g/(2kT)} \quad (3)$$

As we can see, Equation (3) has the same coefficients and form as the computation in Equation (1). The difference is that we also have to account for holes. At thermal equilibrium and intrinsic silicon $n_i^2 = n_0 p_0$

B. How to think about electrons (and holes)

I've come to the realization that to imagine electrons as balls moving around in the silicon crystal is a bad mental image.

For example, for a metal-oxide-semiconductor field effect transistor (MOSFET) it is not the case that the electrons that form the inversion layer under strong inversion come from somewhere else. They are already at the silicon surface, but they are bound in covalent bonds (there are literally trillions of bound electrons in a typical transistor).

What happens is that the applied voltage at the gate shifts the energy bands close to the surface (or bends the bands in relation to the Fermi level), and the density of carriers in the conduction band in that location changes, according to the type of derivations above.

Once the electrons are in the conduction band, then they follow the same equations as diffusion of a gas, [Fick's law of diffusion](#). Any charge density concentration difference will give rise to a [diffusion current](#) given by

$$J_{\text{diffusion}} = -qD_n \frac{\partial \rho}{\partial x} \quad (4)$$

where J is the current density, q is the charge, ρ is the charge density, and D is a diffusion coefficient that through the [Einstein relation](#) can be expressed as $D = \mu kT$, where mobility $\mu = v_d/F$ is the ratio of drift velocity v_d to an applied force F .

To make matters more complicated, an inversion layer of a MOSFET is not in three dimensions, but rather a [two dimensional electron gas](#), as the density of states is confined close to the silicon surface. As such, we should not expect the mobility of bulk silicon to be the same as the mobility of a MOSFET transistor.

V. DOPING

We can change the property of silicon by introducing other elements, something we've called [doping](#). Phosphor has one more electron than silicon, Boron has one less electron. Injecting these elements into the silicon crystal lattice changes the number of free electron/holes.

These days, we usually dope with [ion implantation](#), while in the olden days, most doping was done by [diffusion](#). You'd paint something containing Boron on the silicon, and then heat it in a furnace to "diffuse" the Boron atoms into the silicon.

If we have an element with more electrons we call it a donor, and the donor concentration N_D .

The main effect of doping is that it changes the location of the Fermi level at thermal equilibrium. For donors, the Fermi level will shift closer to the conduction band, and increase the probability of free electrons, as determined by Equation (2).

Since the crystal now has an abundance of free electrons, which have negative charge, we call it n-type.

If the element has less electrons we call it an acceptor, and the acceptor concentration N_A . Since the crystal now has an abundance of free holes, we call it p-type.

The doped material does not have a net charge, however, as it's the same number of electrons and protons, so even though we dope silicon, it does remain neutral.

The doping concentrations are larger than the intrinsic carrier concentration, from maybe 10^{21} to 10^{27} carriers/m³. To separate between these concentrations we use $p-, p, p+$ or $n-, n, n+$.

The number of electrons and holes in a n-type material is

$$n_n = N_D, p_n = \frac{n_i^2}{N_D}$$

and in a p-type material

$$p_p = N_A, n_p = \frac{n_i^2}{N_A}$$

In a p-type crystal there is a majority of holes, and a minority of electrons. Thus we name holes majority carriers, and electrons minority carriers. For n-type it's opposite.

VI. PN JUNCTIONS

Imagine an n-type material, and a p-type material, both are neutral in charge, because they have the same number of electrons and protons. Within both materials there are free electrons, and free holes which move around constantly.

Now imagine we bring the two materials together, and we call where they meet the junction. Some of the electrons in the n-type will wander across the junction to the p-type material, and visa versa. On the opposite side of the junction they might find an opposite charge, and might get locked in place. They will become stuck.

After a while, the diffusion of charges across the junction creates a depletion region with immobile charges. Where as the two materials used to be neutrally charged, there will now be a build up of negative charge on the p-side, and positive charge on the n-side.

A. Built-in voltage

The charge difference will create a field, and a built-in voltage will develop across the depletion region.

The density of free electrons in the conduction band is

$$n = \int_{E_C}^{\infty} N(E) f(E) dE$$

, where $N(E)$ is the density of states, and $f(E)$ is a probability of a electron being in that state (Equation (2)).

We could write the density of electrons on the n-side as

$$n_n = e^{E_{F_n}/kT} \int_{E_C}^{\infty} N_n(E) e^{-E/kT} dE$$

since the Fermi level is independent of the energy state of the electrons (I think).

The density of electrons on the p-side could be written as

$$n_p = e^{E_{F_p}/kT} \int_{E_C}^{\infty} N_p(E) e^{-E/kT} dE$$

If we assume that the density of states, $N_n(E)$ and $N_p(E)$ are the same, and the temperature is the same, then

$$\frac{n_n}{n_p} = \frac{e^{E_{F_n}/kT}}{e^{E_{F_p}/kT}} = e^{(E_{F_n} - E_{F_p})/kT}$$

The difference in Fermi levels is the built-in voltage multiplied by the unit charge.

$$E_{F_n} - E_{F_p} = q\Phi$$

and by substituting for the minority carrier concentration on the p-side we get

$$\frac{N_A N_D}{n_i^2} = e^{q\Phi_0/kT}$$

or rearranged to

$$\Phi_0 = \frac{kT}{q} \ln \left(\frac{N_A N_D}{n_i^2} \right)$$

B. Current

The derivation of current is a bit involved, but let's try.

The hole concentration on the p-side and n-side could be written as

$$\frac{p_p}{p_n} = e^{-q\Phi_0/kT}$$

The negative sign is because the built in voltage is positive on the n-type side

Assume that $-x_{p0}$ is the start of the junction on the p-side, and x_{n0} is the start of the junction on the n-side.

Assume that we lift the p-side by a voltage qV

Then the hole concentration would change to

$$\frac{p(-x_{p0})}{p(x_{n0})} = e^{q(V - \Phi_0)/kT}$$

while on the n-side the hole concentration would be

$$\frac{p(x_{n0})}{p_n} = e^{qV/kT}$$

So the excess hole concentration on the n-side due to an increase of V would be

$$\Delta p_n = p(x_{n0}) - p_n = p_n \left(e^{qV/kT} - 1 \right)$$

The diffusion current density, given by Equation (4) states

$$J(x_n) = -qD_p \frac{\partial p}{\partial x}$$

Thus we need to know the charge density as a function of x . I'm not sure why, but apparently it's

$$\partial p(x_n) = \Delta p_n e^{-x_n/L_p}$$

where L_p is a diffusion length. I think the equation above, the exponential decay as a function of length, is related to the probability of electron/hole recombination, and how the rate of recombination must be related to the excess hole concentration, as such related to [Exponential decay](#).

Anyhow, we can now compute the current density, and need only compute it for $x_n = 0$, so you can show it's

$$J(0) = q \frac{D_p}{L_p} p_n \left(e^{qV/kT} - 1 \right)$$

which start's to look like the normal diode equation. The p_n is the minority concentration of holes on the n-side, which we've before estimated as $p_n = \frac{n_i^2}{N_D}$

We've only computed for holes, but there will be electron transport from the p-side to the n-side also.

We also need to multiply by the area of the diode to get current from current density. The full equation thus becomes

$$I = qAn_i^2 \left(\frac{1}{N_A} \frac{D_n}{L_n} + \frac{1}{N_D} \frac{D_p}{L_p} \right) [e^{qV/kT} - 1]$$

where A is the area of the diode, D_n, D_p is the diffusion coefficient of electrons and holes and L_n, L_p is the diffusion length of electrons and holes.

Which we usually write as

$$I_D = I_S(e^{\frac{V_D}{V_T}} - 1), \text{ where } V_T = kT/q$$

C. Forward voltage temperature dependence

We can rearrange I_D equation to get

$$V_D = V_T \ln \left(\frac{I_D}{I_S} \right)$$

and at first glance, it appears like V_D has a positive temperature coefficient. That is, however, wrong.

First rewrite

$$V_D = V_T \ln I_D - V_T \ln I_S$$

$$\ln I_S = 2 \ln n_i + \ln Aq \left(\frac{D_n}{L_n N_A} + \frac{D_p}{L_p N_D} \right)$$

Assume that diffusion coefficient³, and diffusion lengths are independent of temperature.

That leaves n_i that varies with temperature.

$$n_i = \sqrt{B_c B_v} T^{3/2} e^{\frac{-E_g}{2kT}}$$

where

$$B_c = 2 \left[\frac{2\pi k m_n^*}{h^2} \right]^{3/2} \quad B_v = 2 \left[\frac{2\pi k m_p^*}{h^2} \right]^{3/2}$$

$$2 \ln n_i = 2 \ln \sqrt{B_c B_v} + 3 \ln T - \frac{V_G}{V_T}$$

with $V_G = E_g/q$ and inserting back into equation for V_D

$$V_D = \frac{kT}{q} (\ell - 3 \ln T) + V_G$$

³From the Einstein relation $D = \mu kT$ it does appear that the diffusion coefficient increases with temperature, however, the mobility decreases with temperature. I'm unsure of whether the mobility decreases with the same rate though.

Where ℓ is temperature independent, and given by

$$\ell = \ln I_D - \ln \left(Aq \frac{D_n}{L_n N_A} + \frac{D_p}{L_p N_D} \right) - 2 \ln \sqrt{B_c B_v}$$

From equations above we can see that at 0 K, we expect the diode voltage to be equal to the bandgap of silicon. Diodes don't work at 0 K though.

Although it's not trivial to see that the diode voltage has a negative temperature coefficient, if you do compute it as in [vd.py](#), then you'll see it decreases.

The slope of the diode voltage can be seen to depend on the area, the current, doping, diffusion constant, diffusion length and the effective masses.

Figure 3 shows the V_D and the deviation of V_D from a straight line. The non-linear component of V_D is only a few mV. If we could combine V_D with a voltage that increased with temperature, then we could get a stable voltage across temperature to within a few mV.

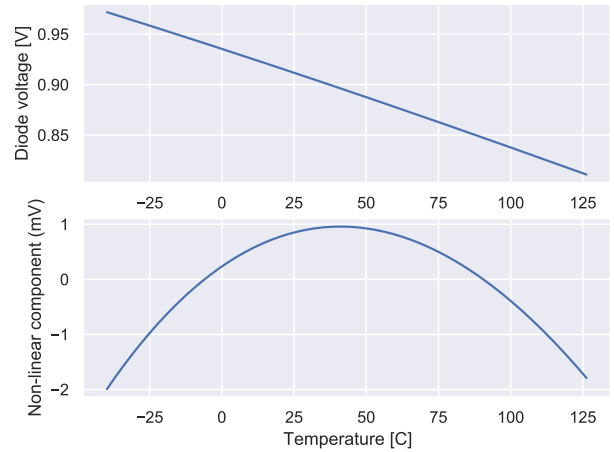


Figure 3: Diode forward voltage as a function of temperature

D. Current proportional to temperature

Assume we have a circuit like Figure 4.

Here we have two diodes, biased at different current densities. The voltage on the left diode V_{D1} is equal to the sum of the voltage on the right diode V_{D2} and voltage across the resistor R_1 . The current in the two diodes are the same due to the current mirror. As such, we have that

$$I_S e^{\frac{qV_{D1}}{kT}} = N I_S e^{\frac{qV_{D2}}{kT}}$$

Taking logarithm of both sides, and rearranging, we see that

$$V_{D1} - V_{D2} = \frac{kT}{q} \ln N$$

Or that the difference between two diode voltages biased at different current densities is proportional to absolute temperature.

In the circuit above, this ΔV_D is across the resistor R_1 , as such, the $I_D = \Delta V_D / R_1$. We have a current that is proportional to temperature.

If we copied the current, and sent it into a series combination of a resistor R_2 and a diode, we could scale the R_2 value to give us the exactly right slope to compensate for the negative slope of the V_D voltage.

The voltage across the resistor and diode would be constant over temperature, with the small exception of the non-linear component of V_D .

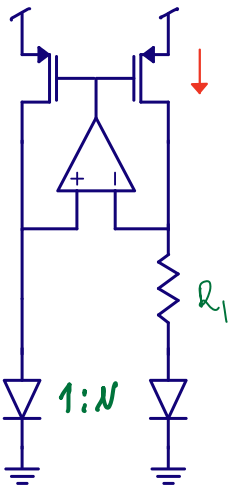


Figure 4: Circuit to generate a current proportional to kT

VII. EQUATIONS AREN'T REAL

Nature does not care about equations. It just is.

We know, at the fundamental level, nature appears to obey the mathematics on quantum mechanics, however, due to the complexity of nature, it's not possible today (which is not the same as impossible), to compute exactly how the current in a diode works. We can get close, by measuring a diode we know well, and hope that the next time we make the same diode, the behavior will be the same.

As such, I want to warn you about the “lies” or “simplifications” we tell you. Take the diode equation above, some parts, like the intrinsic carrier concentration n_i has roots directly from quantum mechanics, with few simplifications, which means it's likely solid truth, at least for a single unit cell.

But there is no reason nature should make all unit cells the same, and infact, we know they are not the same, we put in dopants. As we scale down to a few nano-meter transistors the simplification that “all unit cells of silicon are the same, and

extend to infinity” is no longer true, and must be taken into account in how we describe reality.

Other parts, like the exact value of the bandgap E_g , the diffusion constant D_p or diffusion length L_p are macroscopic phenomena, we can't expect them to be 100 % true. The values would be based on measurement, but not always exact, and maybe, if you rotate your diode 90 degrees on the integrated circuit, the values could be different.

You should realize that the consequence of our imperfection is that the equations in electronics should always be taken with a grain of salt.

Nature does not care about your equations. Nature will easily have the superposition of trillions of electrons, and they don't have to agree with your equations.

But most of the time, the behavior is similar.

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Carsten Wulff received the M.Sc. and Ph.D. degrees in electrical engineering from the Department of Electronics and Telecommunication, Norwegian University of Science and Technology (NTNU), in 2002 and 2008, respectively. During his Ph.D. work at NTNU, he worked on open-loop sigma-

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