

TFE4188 - Introduction to Lecture 9

Oscillators

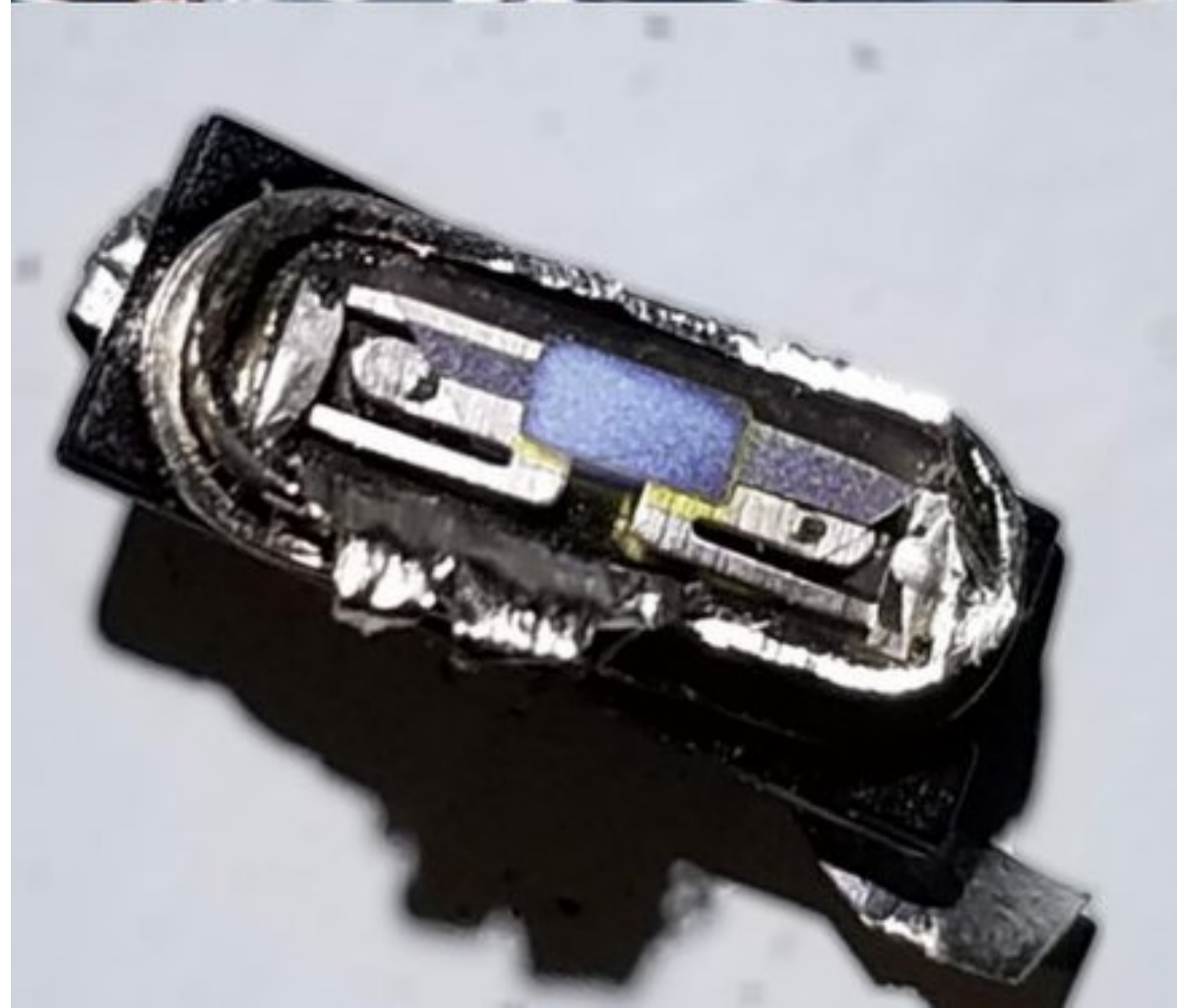
Goal

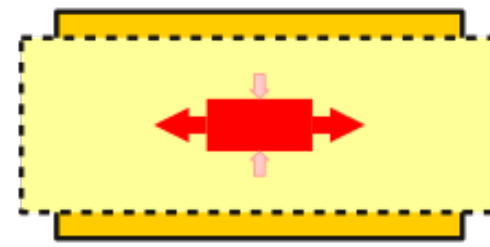
Introduction to **Crystal Oscillators**

Introduction to **VCOs**

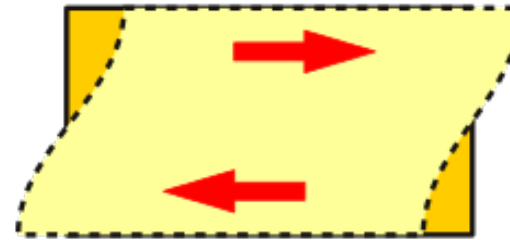
Introduction to **Relaxation-oscillators**

Crystal oscillators

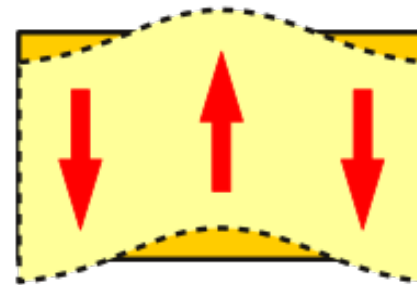




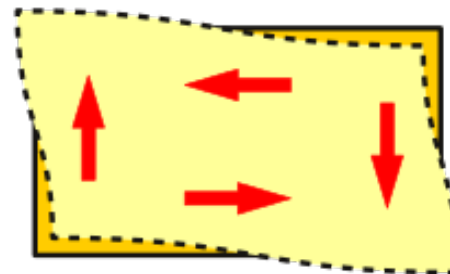
Longitudinal mode



Thickness shear mode



Flexural mode

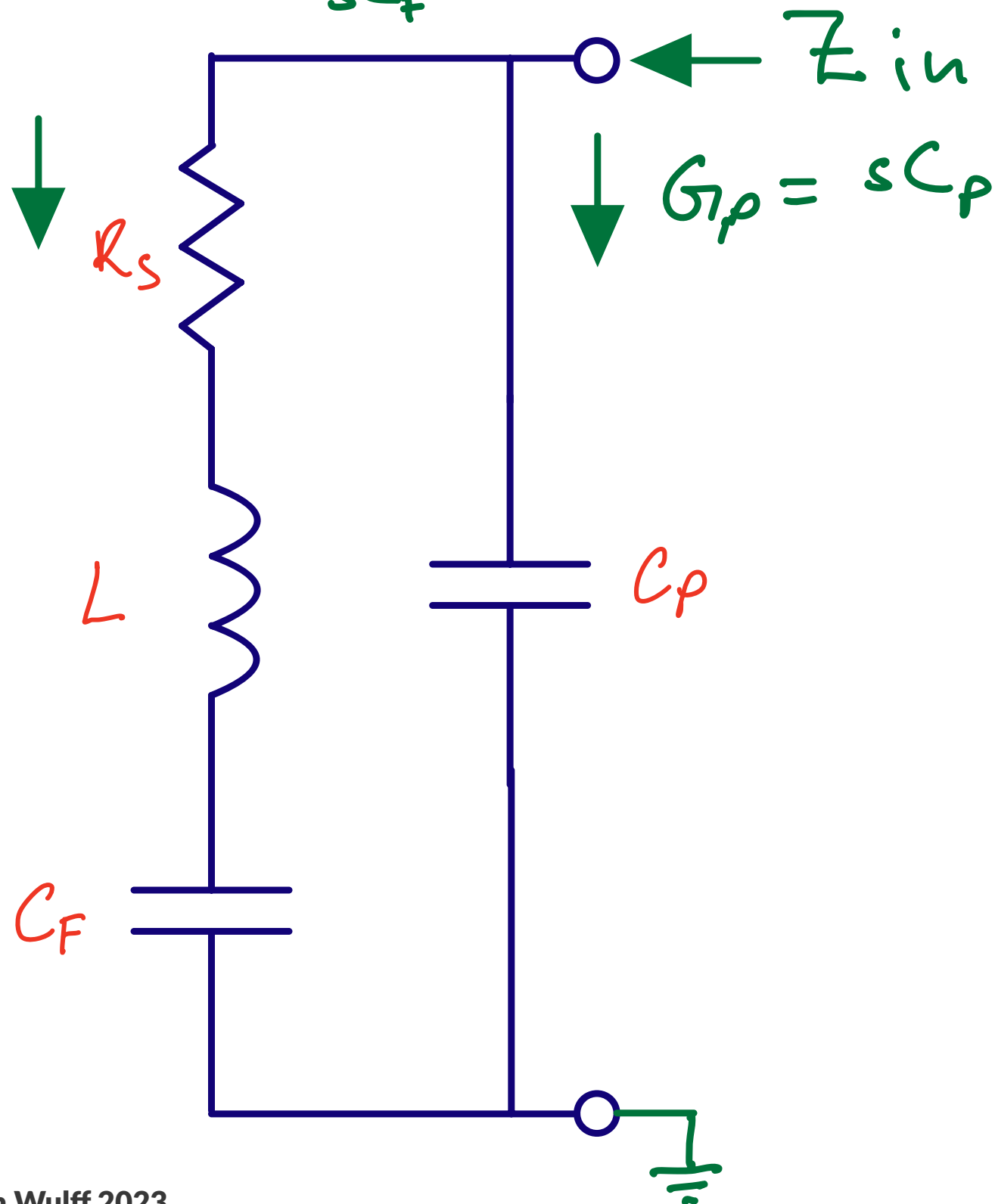


Face shear mode



Tuning fork

$$R = R_s + sL + \frac{1}{sC_F}$$



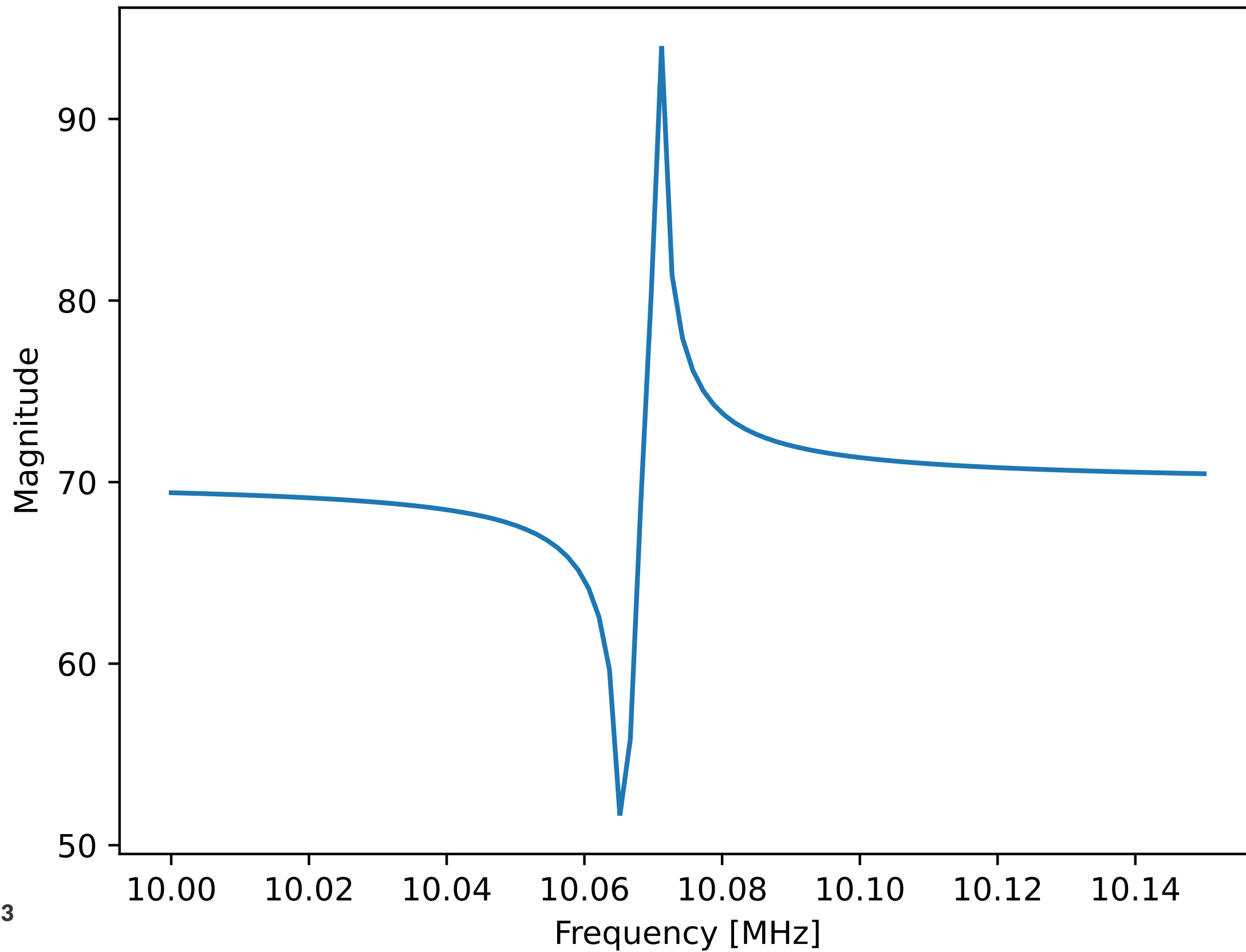
Assuming zero series resistance

$$Z_{in} = \frac{s^2 C_F L + 1}{s^3 C_P L C_F + s C_P + s C_F}$$

Since the $1/(sC_P)$ does not change much at resonance, then

$$Z_{in} \approx \frac{L C_F s^2 + 1}{L C_F C_P s^2 + C_F + C_P}$$

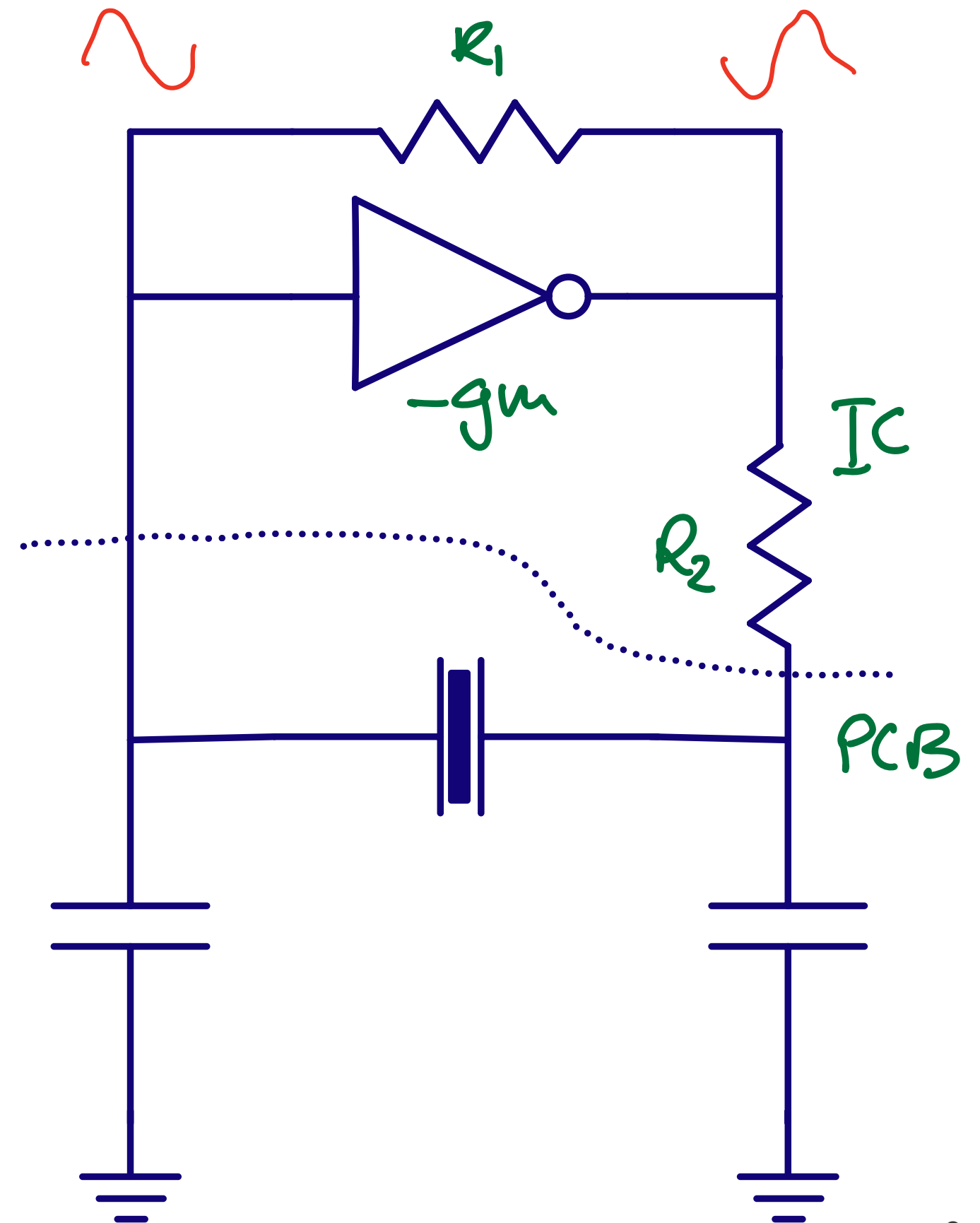
See [Crystal oscillator impedance](#) for a detailed explanation.



Negative transconductance compensate crystal series resistance

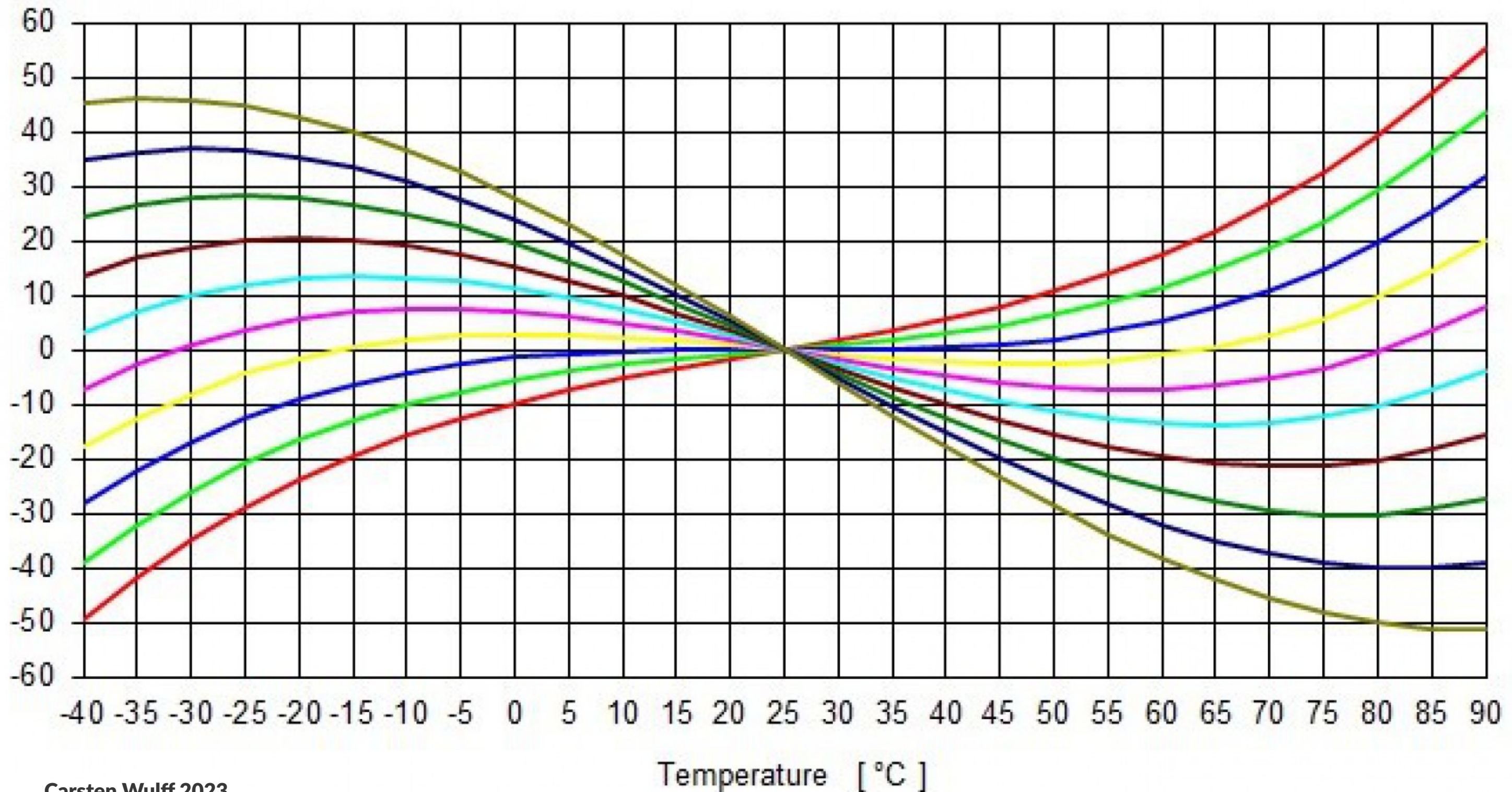
Long startup time caused by high Q

Can fine tune frequency with parasitic capacitance

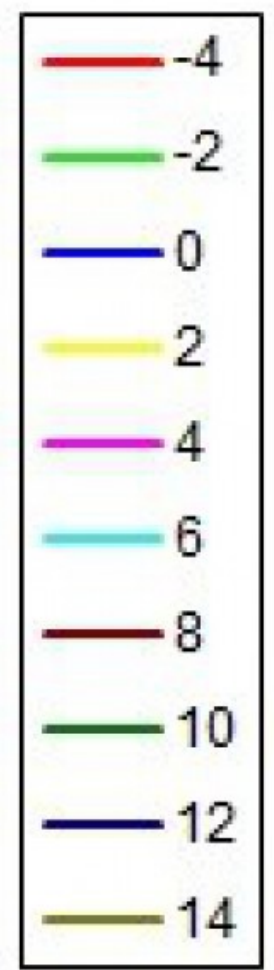


Temperature Behaviour for AT Cut Crystals

df / f [ppm]

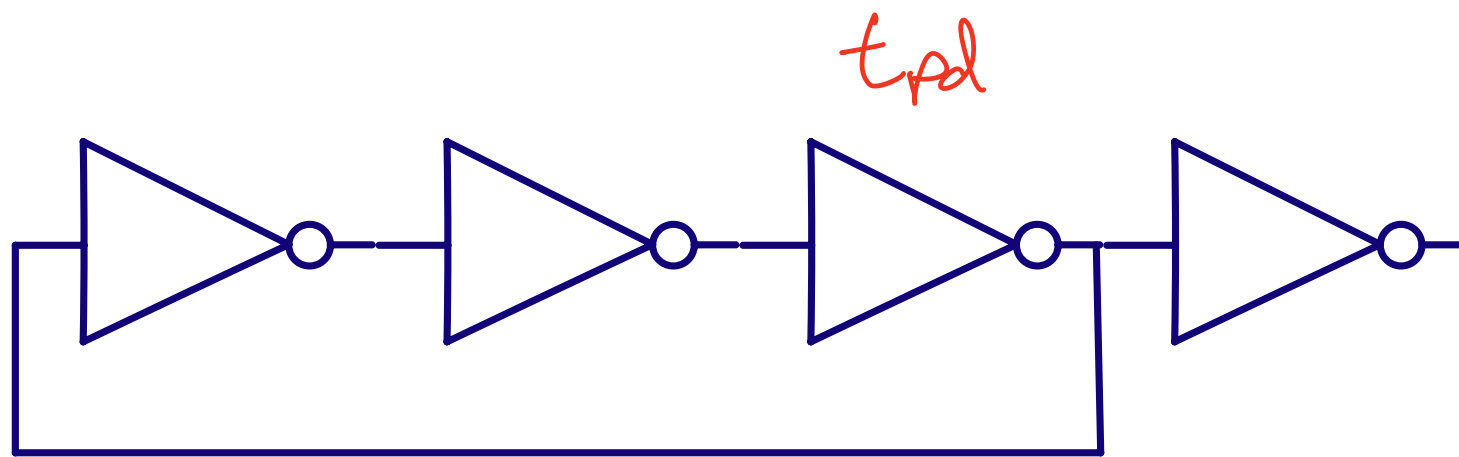


Cutting Angle [min]



Controlled Oscillators

Ring oscillator



$$t_{pd} \approx RC$$

$$R \approx \frac{1}{gm} \approx \frac{1}{\mu_n C_{ox} \frac{W}{L} (V_{DD} - V_{th})}$$

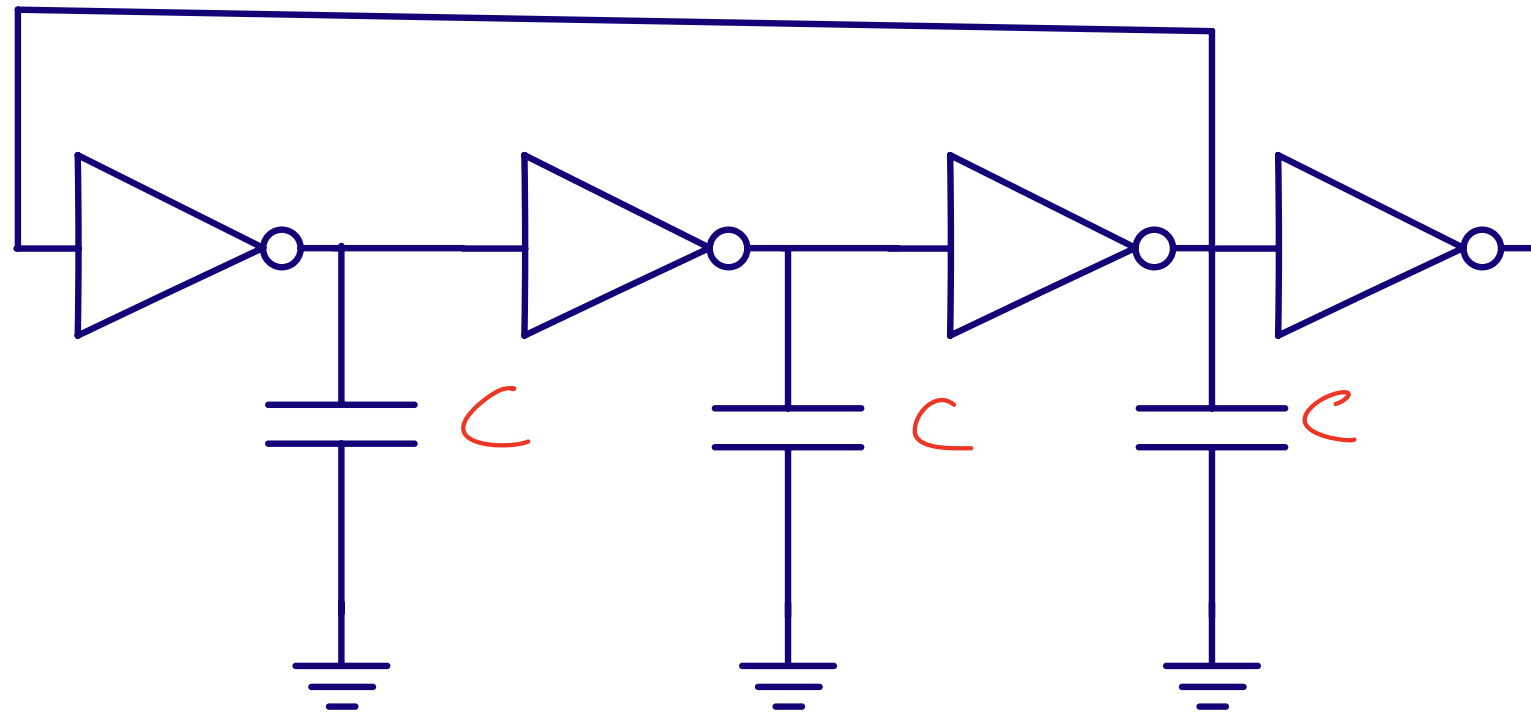
$$C \approx \frac{2}{3} C_{ox} WL$$

$$t_{pd} \approx \frac{2/3 C_{ox} W L}{\frac{W}{L} \mu_n C_{ox} (V_{DD} - V_{th})}$$

$$f = \frac{1}{2N t_{pd}} = \frac{\mu_n (V_{DD} - V_{th})}{\frac{4}{3} N L^2}$$

$$K_{vco} = 2\pi \frac{\partial f}{\partial V_{DD}} = \frac{2\pi \mu_n}{\frac{4}{3} N L^2}$$

Capacitive load



$$f = \frac{\mu_n C_{ox} \frac{W}{L} (V_{DD} - V_{th})}{2N \left(\frac{2}{3} C_{ox} WL + C \right)}$$

$$K_{vco} = \frac{2\pi \mu_n C_{ox} \frac{W}{L}}{2N \left(\frac{2}{3} C_{ox} WL + C \right)}$$

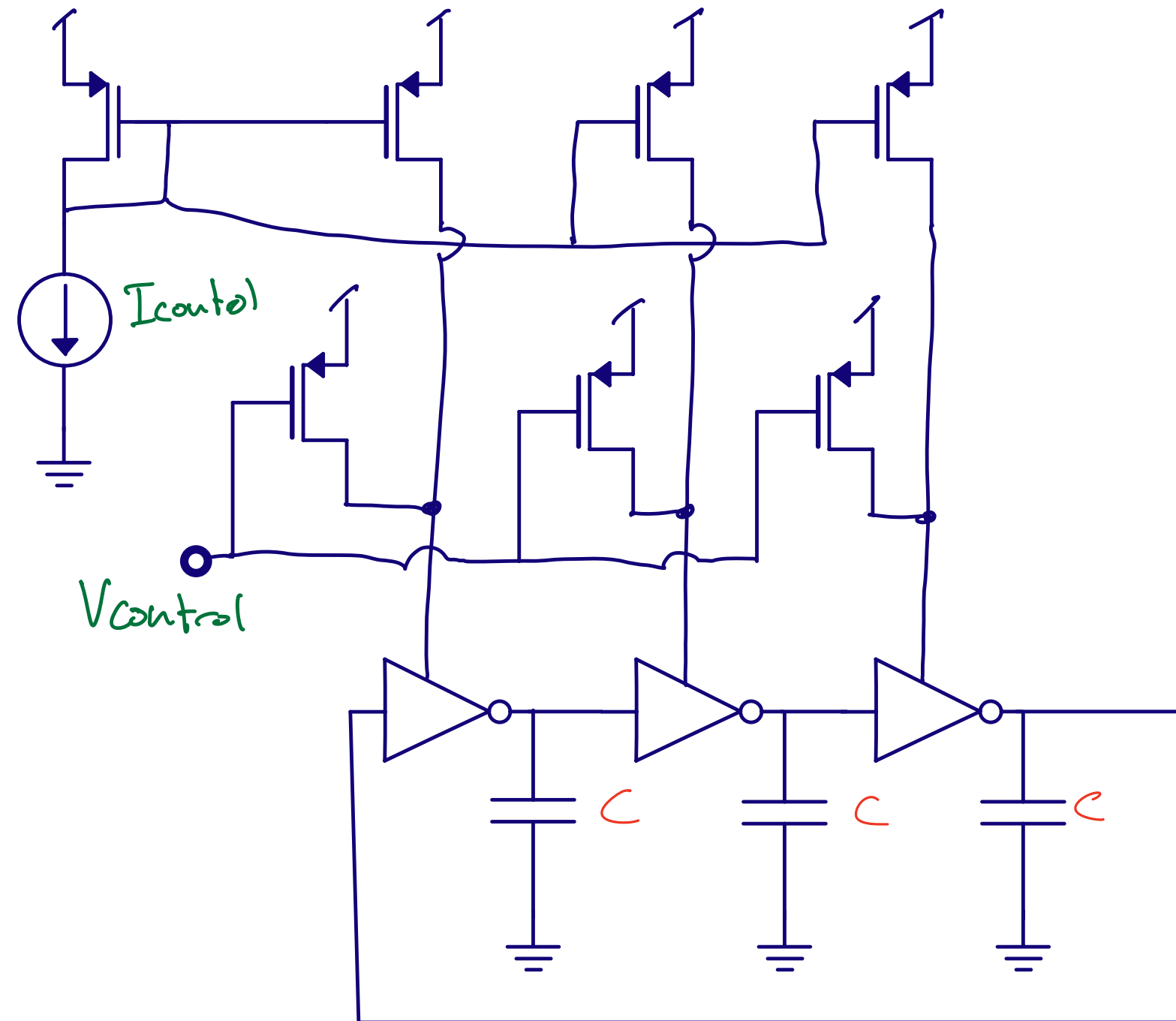
Realistic

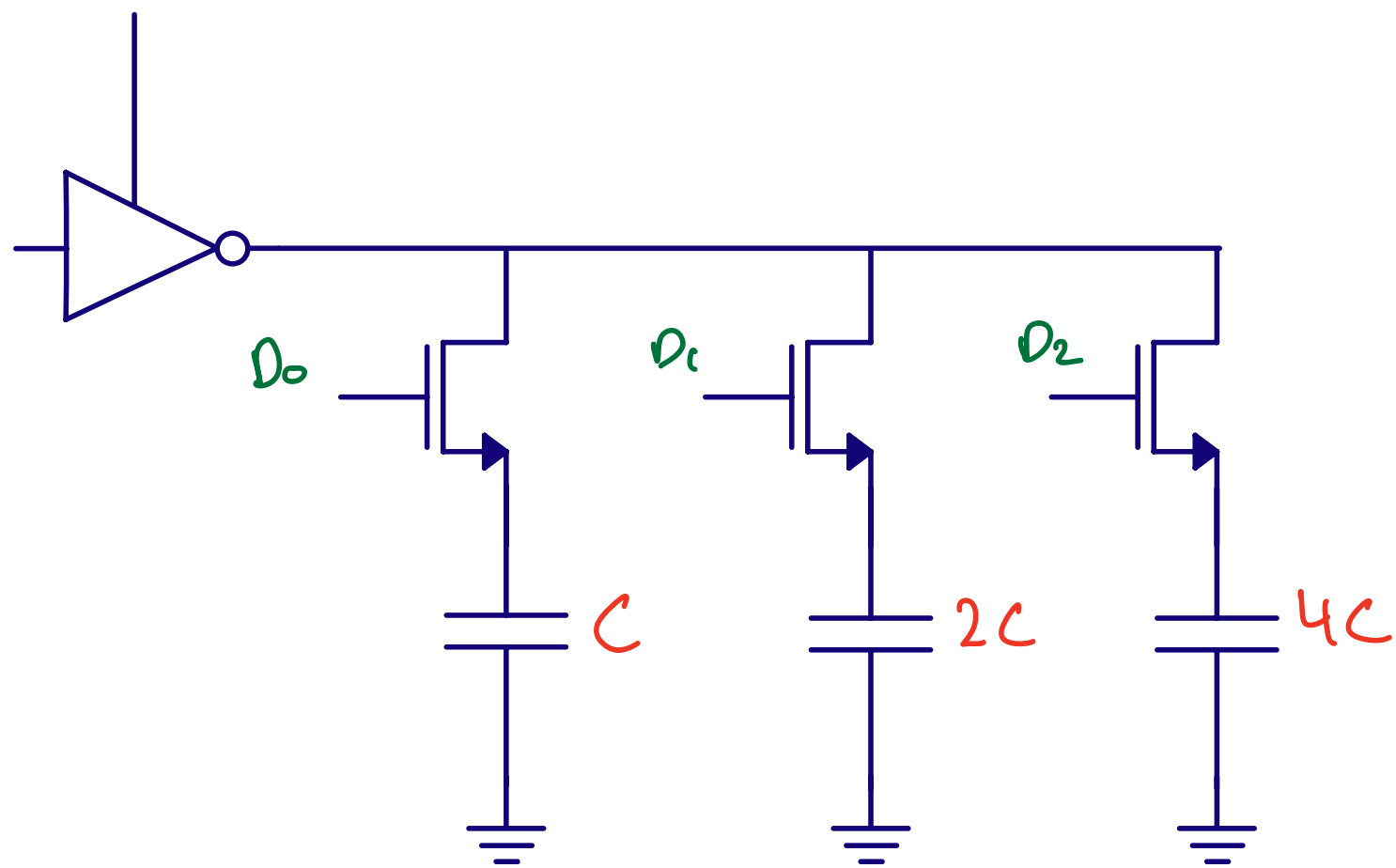
$$I = C \frac{dV}{dt}$$

$$f \approx \frac{I_{control} + \frac{1}{2} \mu_p C_{ox} \frac{W}{L} (V_{DD} - V_{control} - V_{th})^2}{C \frac{V_{DD}}{2} N}$$

$$K_{vco} = 2\pi \frac{\partial f}{\partial V_{control}}$$

$$K_{vco} = 2\pi \frac{\mu_p C_{ox} W/L}{C \frac{V_{DD}}{2} N}$$

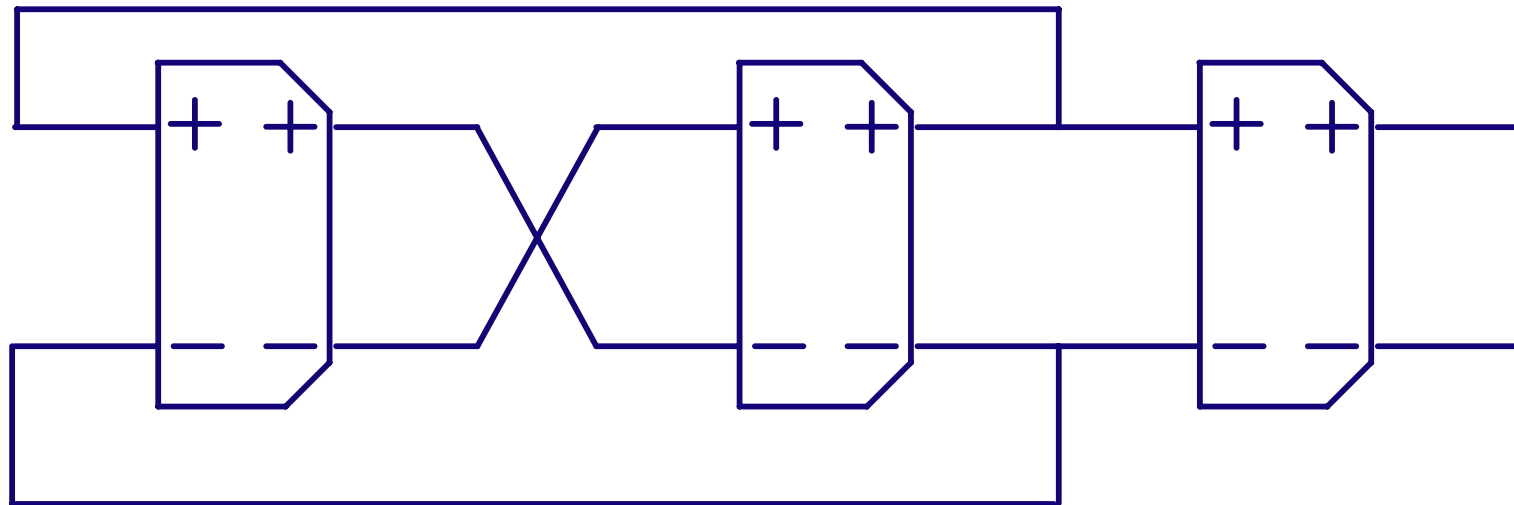


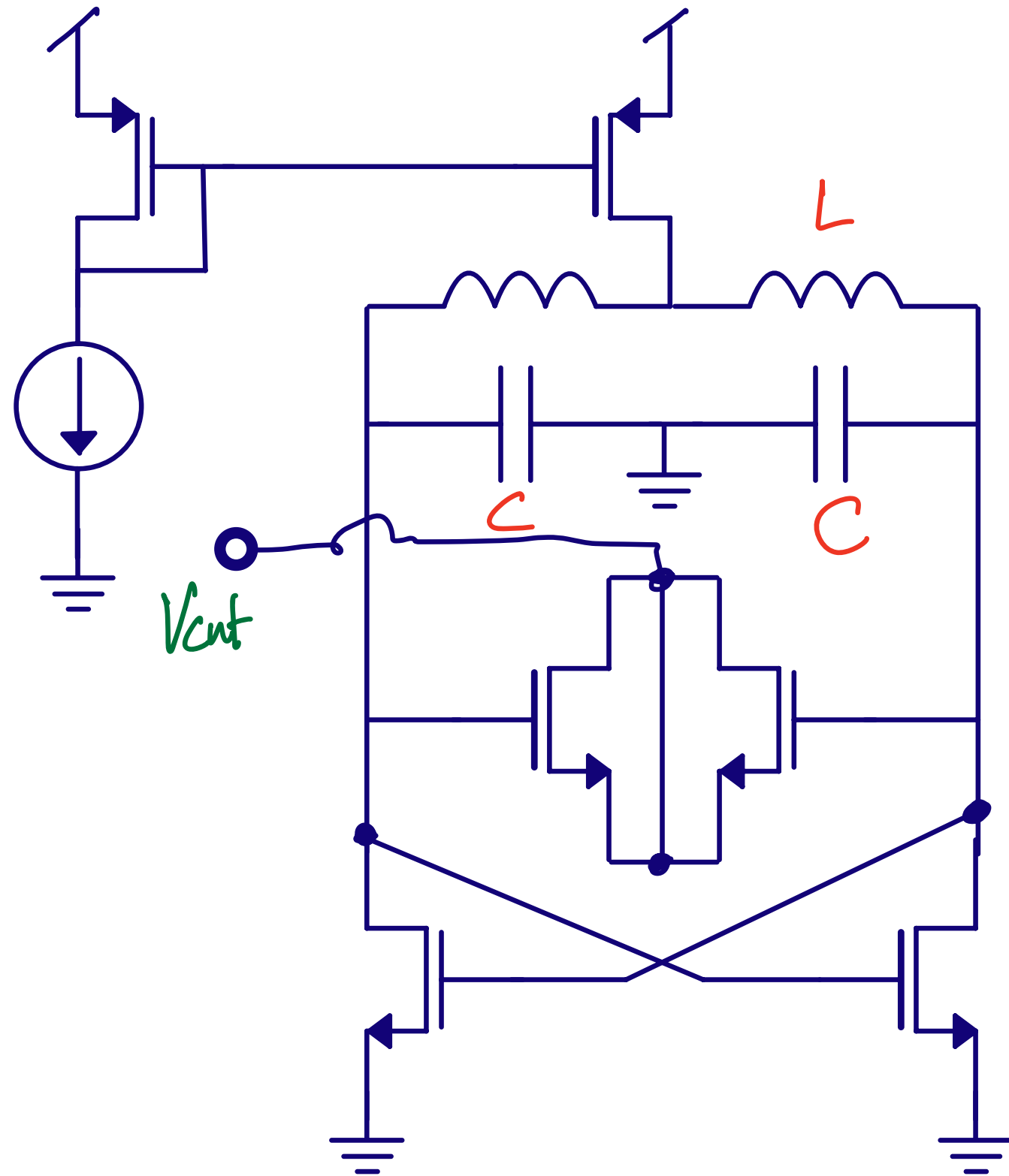


Digitally controlled oscillator

Differential

Potentially less sensitive to supply noise

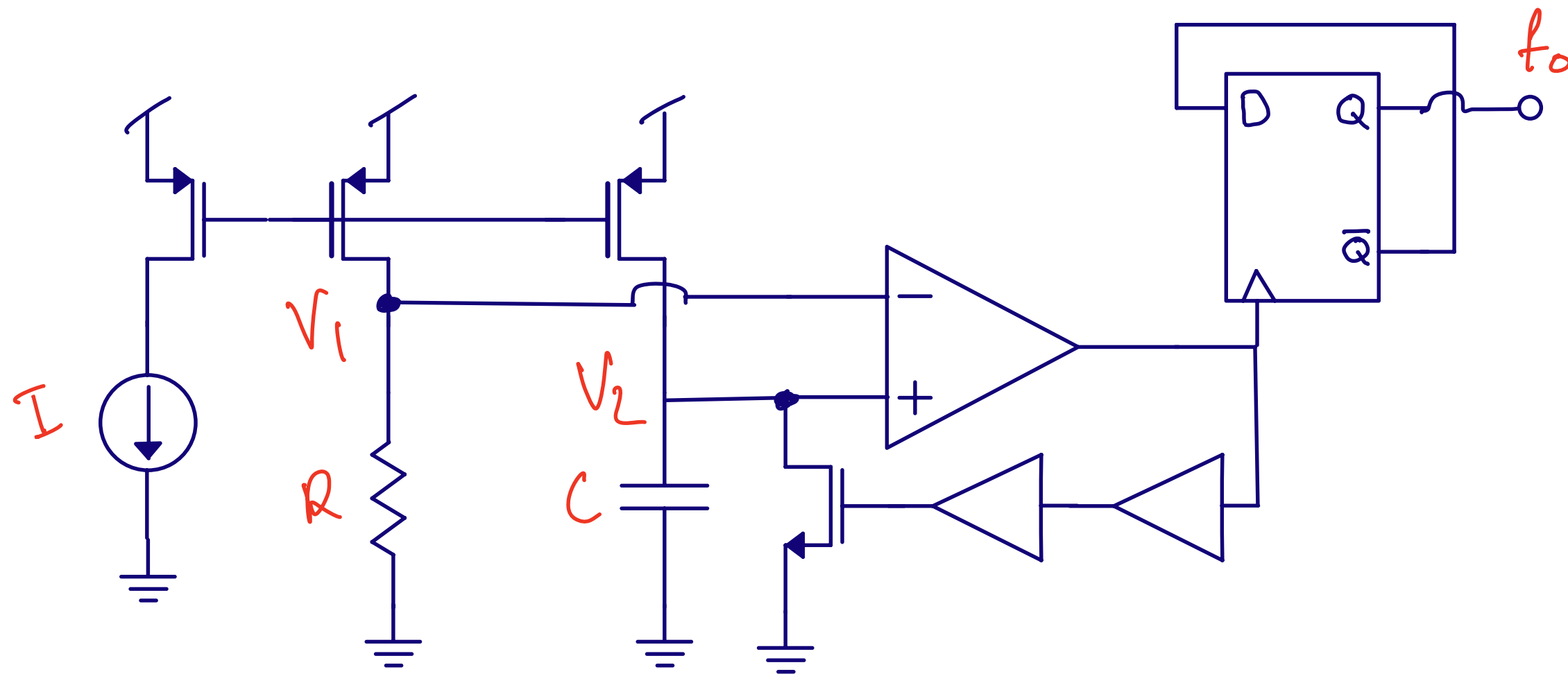




LC oscillator

$$f \propto \frac{1}{\sqrt{LC}}$$

Relaxation oscillators



Q: Show that F_0 is $1/(2RC)$

Additional material

[The Crystal Oscillator - A Circuit for All Seasons](#)

[The Delay-Locked Loop - A Circuit for All Seasons](#)

[The Ring Oscillator - A Circuit for All Seasons](#)

Thanks!